

sec 6.5 7-31-14

(7)

ex 1 \rightarrow 5

2 \rightarrow 5, 7, 9, 11

3 \rightarrow 11 11 11 11

4 \rightarrow 17, 23

(5.)

$$1 + \left(\frac{1}{4}\right)$$

← subfactor

$$2 + \left(\frac{3}{4}\right)$$

METHOD 2

let $= 4$

$$\left[\left(\frac{1}{4}\right) + \left(\frac{3}{4}\right) \right] \cdot 4 = \frac{4 + 12}{4} = \frac{16}{4} = 4$$

of 1, 4, 1, 4

$$\left[\left(\frac{2}{4}\right) + \left(\frac{3}{4}\right) \right] \cdot 4 = \frac{8 + 12}{4} = \frac{20}{4} = 5$$

7-31

6.5

sec 6.5

METHOD 1

(2)

5

$$\frac{1 + \frac{1}{9}}{2 + \frac{3}{9}} = \frac{\frac{1}{1} + \frac{1}{9}}{\frac{2}{1} + \frac{3}{9}} = \frac{\frac{4}{9} + \frac{1}{9}}{\frac{8}{9} + \frac{3}{9}}$$

$$= \frac{\frac{5}{9}}{\frac{11}{9}}$$

$$= \frac{5}{11}$$

7

$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{1}{4} - \frac{1}{6}} \quad \text{METHOD 1}$$

$$\frac{\frac{3}{6} + \frac{2}{6}}{\frac{3}{12} - \frac{2}{12}} = \frac{5/6}{1/12}$$

$$= \frac{5}{6} \cdot \frac{12}{1} = \frac{60}{6} = 10$$

$$= \frac{5}{6} \cdot \frac{12}{1} = \frac{60}{6} = 10$$

METHOD

1.

$$12 \cdot \left[\frac{1}{2} + \frac{1}{3} \right]$$
$$12 \cdot \left[\frac{1}{4} + \frac{1}{6} \right]$$

LCM of 2, 3, 4, 6

$$= 12$$

3

$$\frac{6 + 4}{1} = 10$$

$$3 - 2$$

9.

$$\frac{\frac{x}{4} + x}{\frac{4}{x} + x} = \frac{\frac{x}{4} + \frac{x}{1}}{\frac{4}{x} + \frac{x}{1}}$$

METHOD

LCM = 4

$$\frac{\frac{x}{4} \cdot \frac{1}{1} + \frac{x \cdot 4}{1 \cdot 4}}{\frac{4}{x} \cdot \frac{1}{1} + \frac{x \cdot x}{1 \cdot x}} = \frac{\frac{x + 4x}{4}}{\frac{4 + x^2}{x}}$$

9.

$$\frac{(x+4x)}{4} \cdot \frac{x}{(4+x^2)} = \frac{(5x) \cdot x}{4(4+x^2)}$$

PRIME

$$= \frac{5x^2}{4(4+x^2)}$$

(4)

METHOD 2 :

$$4x^0 \left[\frac{x}{4} + \frac{x}{1} \right]$$

$$4x^0 \left[\frac{4}{x} + \frac{x}{1} \right]$$

$$\frac{x^2 + 4x^2}{16 + 4x^2}$$

$$\frac{16 + 4x^2}{16 + 4x^2}$$

$$\begin{aligned} \text{LCD} &= 4, 1, x, 1 \\ &= 4x \end{aligned}$$

$$\begin{aligned} &= 4 \cdot 1 \cdot 4 \cdot 1 \\ &= 16 \end{aligned}$$

$$\frac{5x^2}{16 + 4x^2}$$

Same!

(11.)

$$\frac{\frac{10}{t}}{\frac{z-5}{t^2-t}} = \frac{\left(\frac{10}{t}\right)}{\left(\frac{z-5}{t^2-t}\right)}$$

METHOD 2: LCD OF t, t^2, t

$$\frac{t^2 \cdot \left(\frac{10}{t}\right)}{t^2 \cdot \left(\frac{z-5}{t^2-t}\right)} = \frac{t \cdot \frac{10}{t}}{t \cdot \frac{z-5}{t^2-t}}$$

$\rightarrow 10t$

$$\frac{10t}{z-5 \cdot t}$$

(6)

METHOD 2:

(17.)

Let D of $S, \cancel{5}, S$
= $\cancel{5} \cdot S$

$$7 = 7$$

$$5 = \cancel{5}$$

$$\frac{[\cancel{5} - \cancel{5}] \cdot (\cancel{5} \cdot S)}{[\cancel{5} - \cancel{5}] \cdot (\cancel{5} \cdot S)}$$

$$\frac{(\cancel{5} - \cancel{5}) \cdot (\cancel{5} \cdot S)}{(\cancel{5} - \cancel{5}) \cdot (\cancel{5} \cdot S)}$$

$$5 - 5$$

$$(\cancel{5} - \cancel{5}) \cdot \cancel{5}$$

$$= \frac{\cancel{5} - \cancel{5}}{\cancel{5}(\cancel{5} - \cancel{5})} = \frac{(\cancel{5} - \cancel{5})}{\cancel{5} \cdot (\cancel{5} - \cancel{5})}$$

$$= \frac{\cancel{5}(\cancel{5} - \cancel{5})}{\cancel{5} \cdot (\cancel{5} - \cancel{5})}$$

$$= \frac{\cancel{5}}{\cancel{5}}$$

Appendix:

$$(a - b) = -(b - a)$$

$$\frac{(a - b)}{(b - a)} = \frac{-(b - a)}{(b - a)} = -1$$

23.

1

$$3. \left[\frac{3}{c^2} + \frac{4}{c} \right]$$

$$\text{LCM of } c^2, c, c^3 \\ = c^3$$

$$c^3 \cdot \left[\frac{6}{c} + \frac{3}{c^3} \right]$$

$$= \frac{7c + 4c^2}{6c^2 - 3}$$

8

6.6

ex 1 \rightarrow (5)

2 \rightarrow 17, (21), 23, 35

(5)

$$\frac{3}{5} - \frac{2}{5} = \frac{x}{6}$$

(5)
 \rightarrow CHECKS.

Let $D=30$

$$30 \left(\frac{3}{5} - \frac{2}{5} \right) = 30 \cdot \frac{x}{6}$$

$$18 - 20 = 5x$$

$$\rightarrow -\frac{2}{5} = x$$

see 6.6

Q

(17)

$$\frac{5}{3t} + \frac{3}{t} = \frac{1}{1}$$

$\frac{14}{3}$ over deck

led of $3t, t, 1 = 3t$

$$3t \left(\frac{5}{3t} + \frac{3}{t} \right) = 3t \cdot \frac{1}{1}$$

$$5 + 9 = 3t$$

$$14 = 3t$$

$$\frac{14}{3} = t$$

00

$$(21) \quad x + \frac{12}{x} = -7$$

$$\frac{x}{1} + \frac{12}{x} = -\frac{7}{1}$$

LCM of 1, x, 1 = x
 $\times \frac{x}{x} = x \cdot \frac{x}{x}$
 $\times \frac{12}{x} = 12 \cdot \frac{x}{x}$
 $\times \frac{-7}{1} = -7 \cdot \frac{x}{x}$
 $= x$

$$x \cdot \left(\frac{x}{1} + \frac{12}{x} \right) = x \cdot \left(-\frac{7}{1} \right)$$

$$\begin{array}{r} x^2 + 12 = -7x \\ +7x \qquad +7x \\ \hline x^2 + 7x + 12 = 0 \end{array}$$

sec. 6.6

all

$$(x+4)(x+3) = 0$$

ff \rightarrow $(x+4) = 0$ OR $(x+3) = 0$
 $x+4 = 0$ OR $x+3 = 0$
 $-4 \quad -4$ $-3 \quad -3$

$$x = -4 \text{ OR } x = -3$$

23

$$\frac{3}{(x-4)} = \frac{5}{(x+1)}$$

method A: cross-multiply
method B: LCD

6.6



$$\underline{A} \quad 3 \cdot (x+1) = 5 \cdot (x-4)$$
$$3x + 3 = 5x - 20$$

$\xrightarrow{-3x}$ $\xrightarrow{-3x}$

$$3 = 2x - 20$$
$$+20 \quad \quad +20$$

$$23 = 2x$$

$$\frac{23}{2} = x$$

23.

sec. 6.6

$$\frac{3}{(x-4)} = \frac{5}{(x+1)}$$

23

$$LCD = (x-4) \cdot (x+1)$$

$$\frac{\cancel{(x-4)} \cdot (x+1) \cdot 3}{\cancel{(x-4)}} = \frac{(x-4) \cdot \cancel{(x+1)} \cdot 5}{\cancel{(x+1)}}$$

$$3(x+1) = 5(x-4)$$

$$\begin{array}{r} 3x + 3 = 5x - 20 \\ -3x \quad -3x \\ \hline \end{array}$$

$$3 = 2x - 20$$

$$23 = 2x$$

$$11.5 = \frac{23}{2} = x$$

6.6

(14)

35.

$$\frac{5}{t-2} + \frac{3t}{t-2} = \frac{4}{t^2 - 8t + 4}$$

$$\frac{5}{(t-2)} + \frac{3t}{(t-2)} = \frac{4}{(t-2)(t-2)}$$

mult of $(t-2)(t-2)$

$$(t-2)(t-2) \left[\frac{5}{(t-2)} + \frac{3t}{(t-2)} \right] = (t-2)(t-2) \cdot \frac{4}{(t-2)(t-2)}$$

$$5(t-2) + 3t \cdot (t-2) = 4$$

$$5t - 10 + 3t^2 - 6t = 4$$

$$3t^2 - t - 10 = 4 \Rightarrow 3t^2 - t - 14 = 0$$

$$3t^2 - t - 14 = 0 \rightarrow (3t - 7)(t + 2) = 0$$

$$\rightarrow 3t - 7 = 0 \text{ OR } t + 2 = 0$$

$$t = \frac{7}{3} - 2$$

P 409 Box

~~0.7~~ EX1
 \rightarrow (3.)

OLIVER
rate

$$\frac{1 \text{ house}}{75 \text{ h}} = \frac{1}{75} \frac{\text{house}}{\text{h}}$$

Pat
rate

$$\frac{1 \text{ house}}{100 \text{ h}} = \frac{1}{100} \frac{\text{house}}{\text{h}}$$

WORK TOGETHER:

$$\text{TOTAL RATE} = \frac{1 \text{ house}}{75 \text{ h}} + \frac{1 \text{ house}}{100 \text{ h}}$$

$$\text{total rate} \cdot t = 1 \text{ house}$$

$$\left(\frac{1}{75} + \frac{1}{100}\right)t = 1$$

$$\left(\frac{1}{75} + \frac{1}{100} \right) \cdot t = \frac{1}{1}$$

0.7

(14)

$$LCD = 300$$

of 75, 100, 1

$$300 \cdot \left(\frac{1}{75} + \frac{1}{100} \right) \cdot t = 300 \cdot \frac{1}{1}$$

$$(4 + 3) \cdot t = 300$$

$$7t = 300$$

$$t = \frac{300}{7} = 42.8$$

$$\begin{array}{r}
 42.8 \\
 \hline
 7 \overline{) 300.0} \\
 \underline{- 280} \\
 20 \\
 \underline{- 14} \\
 60
 \end{array}
 \approx 42.8h$$