

11-13-13 solutions test 2

(1) (1, -2)

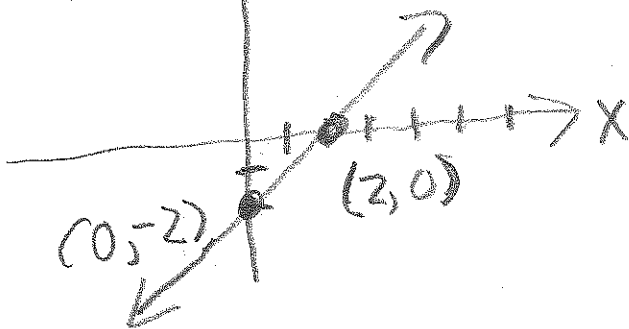
$$6y - 4x = -16$$

$$6(-2) - 4(1) = -16$$

$$-12 - 4 = -16$$

(2)

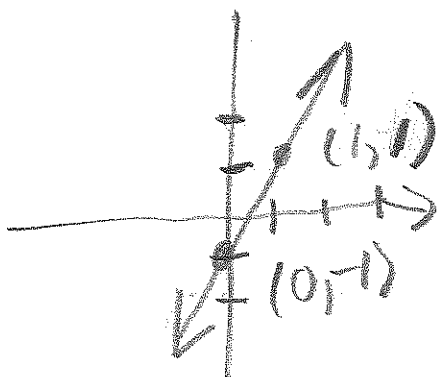
x	y = x - 2
0	-2
2	0



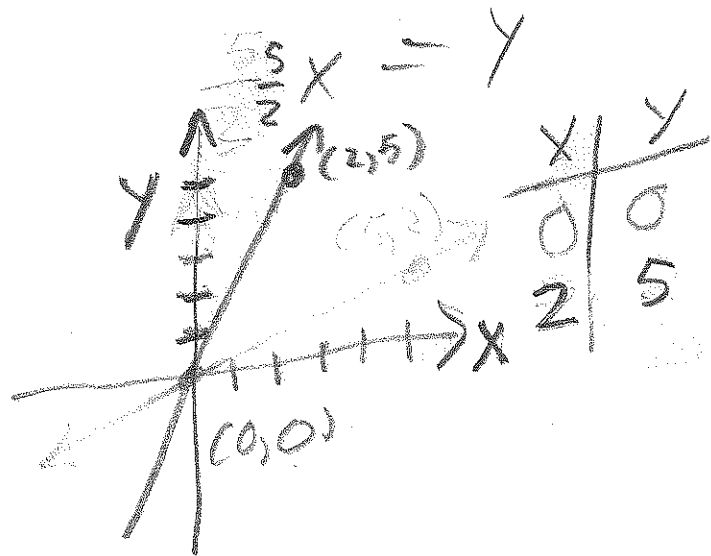
(3)

$$y = 2x - 1$$

x	y
0	-1
1	1



(4) $5x = 2y$

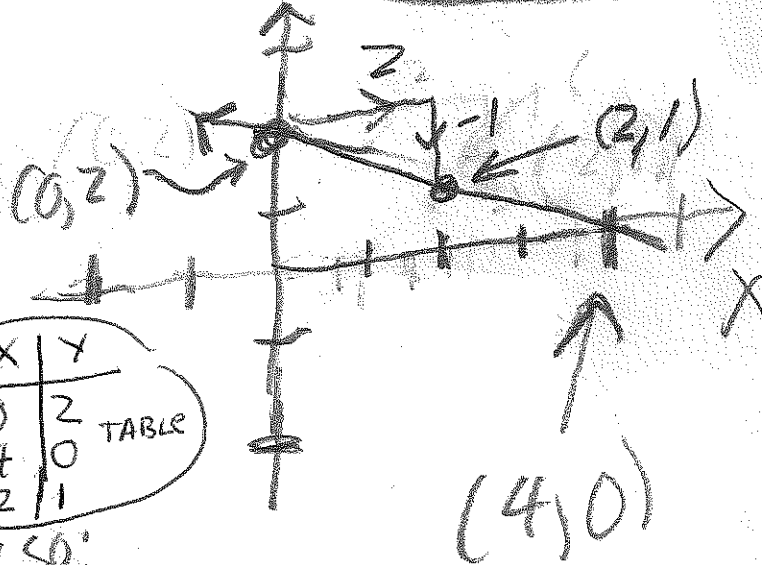


(5)

$$x + 2y = 4$$

$$2y = -x + 4$$

$$y = -\frac{1}{2}x + 2$$



x	y
0	2
4	0
2	1

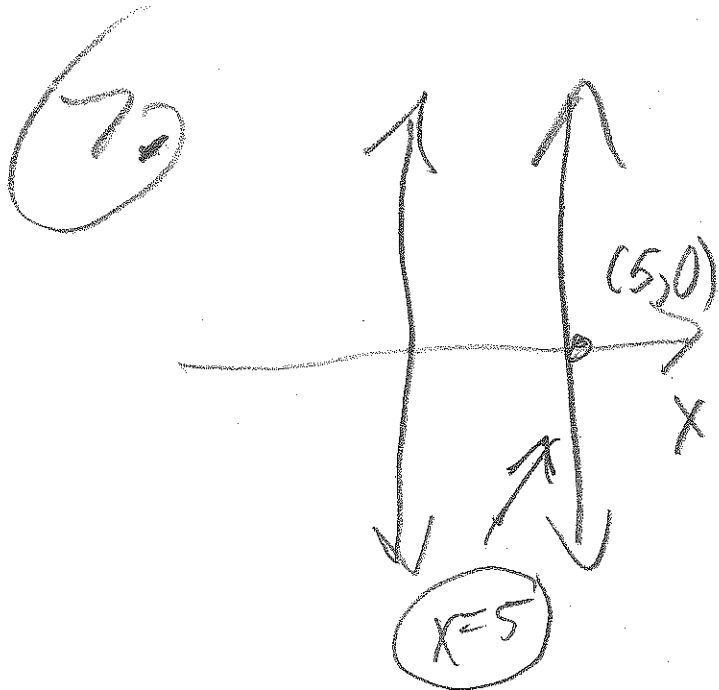
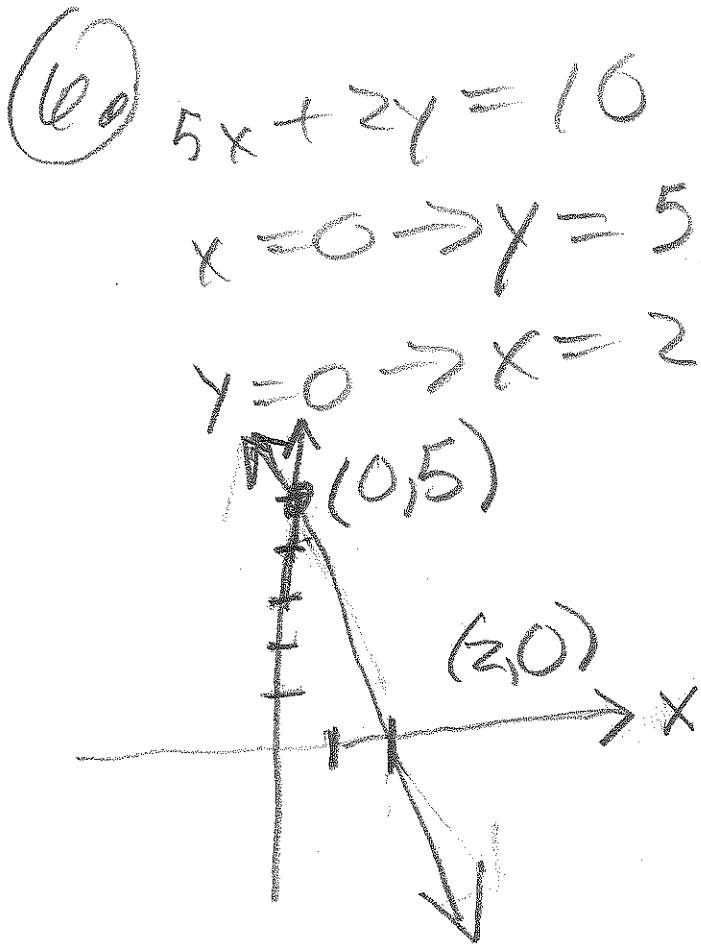
TABLE

ALSO:

USE INTERCEPTS

$$x = 0 \Rightarrow y = 2 \Rightarrow (0, 2)$$

$$y = 0 \Rightarrow x = 4 \Rightarrow (4, 0)$$



(8) $5h$

$$\frac{195}{93} \quad \text{PAY} = 220$$

$$\frac{220}{5h} = \frac{\$44}{h}$$

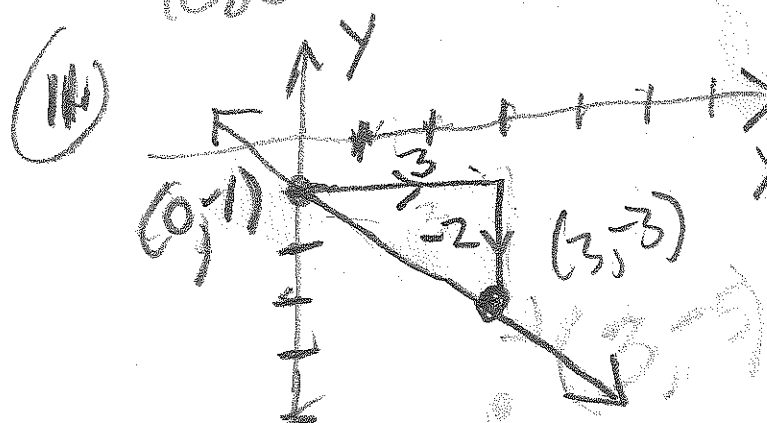
(b) $\frac{\$220}{103 \text{ pg}} = \$2.14/\text{pg}$

$$\begin{array}{r} 2.135 \\ 103 \overline{) 220.000} \\ \underline{206} \\ 140 \\ \underline{103} \\ 370 \\ \underline{309} \\ 610 \end{array}$$

(9) **SHORTCUT**

$$\begin{array}{r} (1, 4) \\ - (3, 0) \\ \hline -2, -2 \Rightarrow \frac{-2}{-2} = 1 \end{array}$$

(10) $\frac{-28}{1080} = \frac{-14}{540} = \frac{-7}{270}$



12.

$$y = -\frac{5}{3}x + 3$$

$$y = mx + b$$

16.

$$x + y = 5$$

$$y = x + 1$$

$$x + x + 1 = 5$$

$$2x + 1 = 5$$

$$2x = 4$$

$$x = 2$$

$$y = 2 + 1 = 3$$

$$\Rightarrow (2, 3)$$

13.

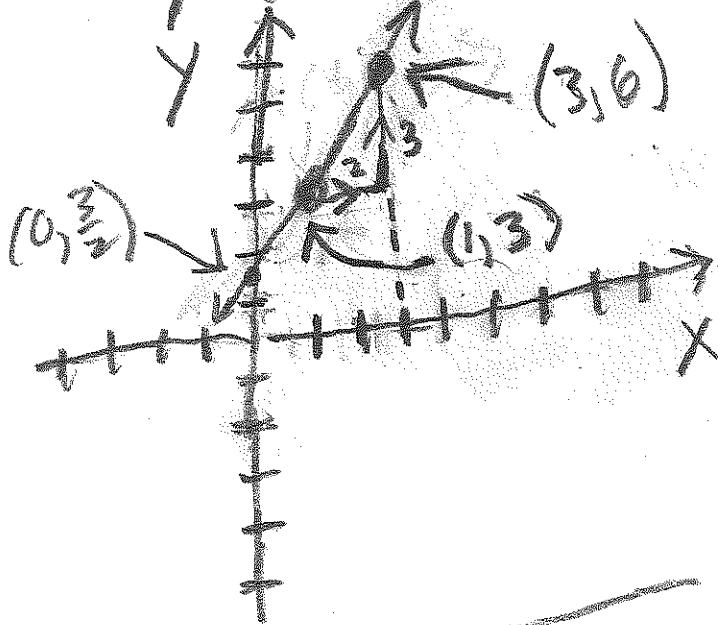
$$y - 5 = 3(x - 5)$$

$$y - 5 = 3(x - (-5))$$

14.

$$(x_1, y_1) = (1, 3)$$

$$y - 3 = \frac{3}{2}(x - 1)$$



17.

$$x = y - 6$$

$$3x + 2y = 2$$

$$3(y - 6) + 2y = 2$$

$$3y - 18 + 2y = 2$$

$$5y = 20$$

$$y = 4 \quad \left. \begin{array}{l} \\ \end{array} \right\} (-2, 4)$$

$$x = -2$$

$$x = 4 - 6 = -2$$

15. (T) $5 \cdot 1 - 2 \cdot 4 = -3$

(T) $7 \cdot 1 - 3 \cdot 4 = -5$

yes!

(18)

$$\left. \begin{array}{l} x - y = 2 \\ x + y = 4 \end{array} \right\} \underline{\text{ADD}}$$

ELIMINATE
y

$$\begin{array}{r} 2x = 6 \\ = 3 \\ \hline y = 1 \end{array}$$

$\Rightarrow (3, 1)$

(19)

$$(x - y = 3) \cdot 2$$

$$2x - 2y = 6$$

$$(2x - 3y = -1)$$

$$y = 7$$

$$x - y = 3$$

$$x - 7 = 3$$

$$x = 10$$

$$(10, 7)$$

(20)

$$\begin{array}{l} x + y = 200 \\ 0.50x + 0.80y = 136 \end{array}^*$$

* $136 = (0.68)(200)$

$$\begin{array}{r} x + y = 200 \\ 50x + 80y = 13600 \end{array}$$

$$x = 200 - y$$

$$50(200 - y) + 80y = 13600$$

$$10000 - 50y + 80y = 13600$$

$$= 50 + 30y = 3600$$

$$30y = 3600$$

$$y = 120$$

$$x = 80$$

SOLUTION

$$(80, 120)$$

18.

$$x - y = 2$$

$$x + y = 4$$

19.

$$x - y = 3$$

$$2x - 3y = -1$$

SOLVE USING THE SUBSTITUTION OR ELIMINATION METHOD:

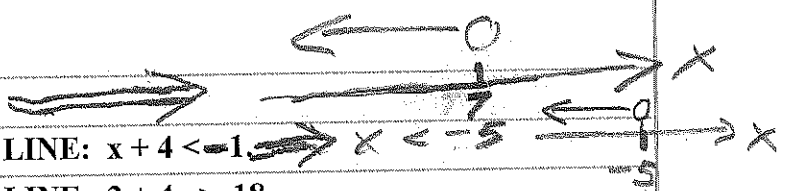
20. JEROME'S EXPERIMENT REQUIRES HIM TO MIX A 50 % ACID SOLUTION WITH AN 80 % ACID SOLUTION TO CREATE 200 -oz OF A 68 % ACID SOLUTION. HOW MUCH 50 % SOLUTION (called x) AND HOW MUCH 80 % ACID SOLUTION (called y) SHOULD HE USE? IN OTHER WORDS, SOLVE FOR x AND y.

SEC. 2.6 AND 2.7

21. FOR EACH PART BELOW, DETERMINE WHETHER EACH NUMBER IS A SOLUTION TO THE INEQUALITY: SUBSTITUTE THE NUMBER INTO THE INEQUALITY. IF THE NUMBER IS A SOLUTION WRITE "YES"; IF NOT WRITE "NO".

$x < 19$ T F F
(a) 18.99 (b) 19.01 (c) 19

22. GRAPH ON A NUMBER LINE: $x < 7$.



23. SOLVE AND GRAPH ON A NUMBER LINE: $x + 4 < -1$.

24. SOLVE AND GRAPH ON A NUMBER LINE: $2 + 4x > 18$

25. RJ'S PLUMBING AND HEATING CHARGES \$55 PLUS \$40 PER HOUR FOR EMERGENCY SERVICE. CHARLOTTE REMEMBERS BEING BILLED AT LEAST \$150 FOR AN EMERGENCY CALL. HOW LONG (IN HOURS) WAS RJ'S SERVICE AT HER HOME?

26. EXTRA CREDIT: LESLIE'S FIRST FOUR QUIZ GRADES ARE 73, 75, 89 AND 91. SHE WANT TO EARN AN AVERAGE OF AT LEAST 85 % . WHAT SCORE ON THE 5TH QUIZ WILL HER AVERAGE QUIZ GRADE BE AT LEAST 85?

26.
$$\frac{73 + 75 + 89 + 91 + x}{5} \geq 85$$

$$\frac{328 + x}{5} \geq 85 \Rightarrow 328 + x = 425 \Rightarrow x = 97$$

24.
$$2 + 4x > 18$$

$$4x > 16$$

$$x > 4$$

A number line graph for $x > 4$ is shown with an open circle at 4 and an arrow pointing to the right.

25.
$$215 \leq 55 + 40 \cdot t$$

$$160 \leq 40t$$

$$4h < t$$

4.7 grid

EX

problem

1 → 1

2 → 7

3 → 9

4 → 17, 29, 19

5 → 35

4.8 GRID

EX

problem

1

5, 7

2

27, 29

3

33, 38, 47, 53

4

63

5

77

11-13-13 4.6, 4.7, 4.8 E.C. on Test #3*

BRID 4.6

<u>EX</u>	<u>prob</u>
1	9
2	13
3	21
4	29
5	33, 41, 39
6	39
7	65
8	(47, 51, 55) 57

for Test 3

*Test 3 = 7.5, 7.6, 7.7, 4.1-4.6
E.C.

ALSO E.C. 4.7, 4.8

4.6

(47) FOIL

$$(xy - 1)(xy + 5)$$

Diagram illustrating the FOIL method for $(xy - 1)(xy + 5)$. The first term of the first binomial is xy (labeled 'F'), the first term of the second binomial is xy (labeled 'O'), the second term of the first binomial is -1 (labeled 'I'), and the second term of the second binomial is 5 (labeled 'L'). Arrows indicate the multiplication of these terms: $xy \cdot xy$, $xy \cdot 5$, $-1 \cdot xy$, and $-1 \cdot 5$.

$$\begin{aligned} & xy \cdot xy \\ &= (xy)(xy) \\ &= (xy)^2 \end{aligned}$$

F O I L

$$(xy)^2 + 5xy - xy - 5$$

$$\begin{aligned} & \rightarrow x^2 \cdot y^2 \\ &= (xy)^2 \end{aligned}$$

$$= x^2 y^2 + 4xy - 5$$

$$= (xy)^2 + 4xy - 5$$

(57) $(pq + 0.1)(pq + 0.1)$

Diagram illustrating the FOIL method for $(pq + 0.1)(pq + 0.1)$. The first term of the first binomial is pq (labeled 'F'), the first term of the second binomial is pq (labeled 'O'), the second term of the first binomial is 0.1 (labeled 'I'), and the second term of the second binomial is 0.1 (labeled 'L'). Arrows indicate the multiplication of these terms: $pq \cdot pq$, $pq \cdot 0.1$, $0.1 \cdot pq$, and $0.1 \cdot 0.1$.

$$-p^2 q^2 + 0.1pq - 0.1pq + (0.1)^2$$

F O I L

$$(57) \quad -p^2q^2 + (0.1)^2 = -p^2q^2 + 0.01$$

$$(0.1)^2 = 0.1 \cdot 0.1 \\ = 0.01$$

$0.1 \leftarrow 2 \text{ digits behind.}$
 $\times \frac{0.1}{0.01}$
 $\leftarrow 2 \text{ places}$

(51)

$$(5rt - 2) \cdot (4rt - 3)$$

$$20 \cdot r^2 \cdot t^2 - 15rt - 8rt + 6$$

F O I L

(51.)

$$20r^2t^2 - 23rt + 6$$

(55.)

$$(6x - 2y) \cdot (5x - 3y)$$

F

O

I

L

$$30x^2 - 18xy - 10xy + 6y^2$$

$$= 30x^2 - 28xy + 6y^2$$

$$\underline{\underline{4.7}} \quad \text{E.C. T3}$$

$$\underline{\underline{4.8}} \quad \text{E.C. T3}$$

$$\textcircled{1} \quad \frac{40x^6 - 25x^3}{5}$$

$$= \frac{40x^6}{5} - \frac{25x^3}{5}$$

$$= 8x^6 - 5x^3$$

$$\textcircled{7.} \quad (42x^5 - 36x^3 + 9x^2) \div (6x^2)$$

$$\frac{x^5}{x^2} = x^3$$

=

$$\frac{42x^5 - 36x^3 + 9x^2}{6x^2}$$

$$= 7x^3 - 6x + \frac{3}{2}$$

$$\frac{x^3}{x^2} = x$$
$$\frac{x^2}{x^2} = 1$$

$$\frac{x^2}{x^2} = x^0$$
$$\frac{x^2}{x^2} = 1$$

NEXT

4.7

(17) (29)

(17.) $(x^2 - 8x + 12) \div (x - 2)$

LONG HAND DIVISION

(1) $\frac{x^2}{x} = x$

(2) $x \cdot (x - 2)$
 $= x^2 - 2x$

(3) $\frac{-6x}{x} = -6$

(4) $-6 \cdot (x - 2)$
 $= -6x + 12$

(5) $\frac{-6x + 12}{x - 2}$

(6) $\frac{-6x + 12}{x - 2}$

(7) $\frac{-6x + 12}{x - 2}$

(8) $\frac{-6x + 12}{x - 2}$

(9) $\frac{-6x + 12}{x - 2}$

ANSWER!
 $x - 6$

OLD SKOOL

$$\begin{array}{r}
 53.3 \dots \\
 \hline
 6 \overline{) 3200} \\
 \underline{- 30} \\
 20 \\
 \underline{- 18} \\
 20
 \end{array}$$

$$3a + 1 \quad R3$$

(29)

(2a)

$$\begin{array}{r}
 (2a + 5) \overline{) 6a^2 + 17a + 8} \\
 \underline{-(6a^2 + 15a)} \\
 2a + 8 \\
 \underline{-(2a + 5)} \\
 3
 \end{array}$$

(1) $\frac{6a^2}{2a} = 3a$

(2) $3a \cdot (2a + 5)$
 $6a^2 + 15a$

(3) $6a^2 + 17a$
 $\underline{-(6a^2 + 15a)}$
 $2a$

(6) $2a + 8$
 $\underline{-(2a + 5)}$
 3

$2a + 8$
 $\underline{-(2a + 5)}$
 3

(4)

$\frac{2a}{2a} = 1$

(5) $1 \cdot (2a + 5)$
 $= 2a + 5$

Quiz 7, 8, 9

Quiz 7

10-25-13 link

Quiz 8

11-04-13 link

Quiz 9

11-06-13 link

↑
SAMPLES EXAM

Quiz 7 study

5 to 12. by seeing

LINKS to lecture

on 7.5 → send LINKS

Quiz 7 1-4 sec 7.6

→ send links

send you a special

PAGE:

- ① LINKS TO LECTURES
ON 7.5, 7.6
(QUIZ 7 and QUIZ 8)
- ② LINKS TO QUIZ 7, 8, 9
- ③ LINK TO SOLUTIONS
TO QUIZ 8, 9 (REGULAR
credit stuff)
- ④ LINK TO TONIGHT'S
LECTURE ON 4.6, 4.7
E.C.

Quiz 8 REGULAR CREDIT

7.7, 4c1

7.7

(5.)

DIRECT VARIATION: $Y = k \cdot X$

$$Y = 30 \text{ when } X = 3$$

$$30 = k \cdot 3$$

$$10 = k$$

$$Y = 10 \cdot X$$

FOLLOW UP: FIND Y WHEN X = 6

$$Y = 10 \cdot 6 = \textcircled{60}$$

(6)

$$Y = 500 \text{ when } X = 60$$

$$500 = k \cdot 60$$

$$\frac{500}{60} = k = 8.3$$

$$Y = 8.3 \cdot X$$

$$\frac{500}{60}$$

$$\begin{array}{r} 8.33\overline{3} \\ 6 \overline{) 50.00} \\ \underline{48} \\ 20 \\ \underline{18} \\ 20 \end{array}$$

inverse variation

$$y = \frac{k}{x}$$

(4.) $y = 8$ when $x = 3$

$$8 = \frac{k}{3}$$

$$3 \cdot 8 = \cancel{3} \frac{k}{\cancel{3}}$$

$$24 = k$$

$$y = \frac{24}{x}$$

follow $y = ?$ when $x = 2$

$$y = \frac{24}{2} = 12$$

(8)

$$y = \frac{k}{x}$$

$$0.2 = \frac{k}{5}$$

$$5 \cdot 0.2 = 5 \cdot \frac{k}{5}$$

$$1 = k$$

$$y = \frac{1}{x}$$

9a

$$(9) \quad (a) \quad 8^4 \cdot 8^3 \neq 8^{12}$$
$$= 8^7; \quad 4+3=7$$

$$(c) \quad \frac{(3m)^9}{(3m)^8} = (3m)^{9-8} = (3m)^1$$
$$= 3m$$

(b) on next page

9

(b)

$$\frac{a^{10} \cdot b^{12}}{a^2 \cdot b^0}$$

$$= a^{10-2} \cdot b^{12-0}$$

$$= a^8 \cdot b^{12}$$

ALT-1

$$\frac{a^{10} \cdot b^{12}}{a^2 \cdot 1}$$

$$) \quad b^0 = 1$$

$$= a^8 \cdot b^{12}$$

$$\frac{a^8 \cdot b^{12}}{1} = b^{12}$$

(10) (a) $(8+5)^0 = 1 = (13)^0 = 1$

(b) $(a^5)^8 = a^{5 \cdot 8} = a^{40}$

(c) $(-4m^4)^2 = (-4)^2 \cdot (m^4)^2$

$$= 16 \cdot m^8$$

$$(ab)^n = (a)^n (b)^n$$

(11)

(a)

$$ca^4b^0 \cdot (a^2b)^5$$

$$= (a^4 \cdot b^0) \cdot (a^2)^5 \cdot (b)^5$$

see # 10 (c)

$$= a^4 \cdot b^0 \cdot a^{10} \cdot b^5$$

$$= a^{14} \cdot b^{11}$$

$$a^4 \cdot a^{10} = a^{14}$$

$$b^0 \cdot b^5 = b^5$$

(b) $\left(\frac{4x}{3}\right)^3$

$$= \frac{(4x)^3}{3^3} = \frac{4^3 \cdot x^3}{3^3}$$

$$= \frac{64 \cdot x^3}{27}$$

$$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$$

$$(ab)^n = a^n b^n$$

12.)

$$\left(\frac{-4p^5}{3m^2n^3} \right)^3$$

Don't panic

$$\left(\frac{a}{b} \right)^n = \frac{a^n}{b^n}$$

$$= \frac{(-4p^5)^3}{(3 \cdot m^2 \cdot n^3)^3}$$

$$(ab)^n = a^n b^n$$

$$= \frac{(-4)^3 \cdot (p^5)^3}{3^3 \cdot (m^2)^3 \cdot (n^3)^3}$$

$$= \frac{-64 \cdot p^{15}}{27 \cdot m^6 \cdot n^9}$$

see #11(a)

$$9x^8 - 6x^4 + 6x^2 + 66 + 8x^7 + 2x$$

$$= 9x^8 + 8x^7 - 6x^4 + 6x^2 + 2x + 66$$

4.3

(4.)

$$(2x^2 - 4x + 15) + (20x^2 + 14x - 14)$$

$$= 22x^2 + 10x + 1$$

change signs

(5.)

$$(2x^2 - 4x + 15) - (20x^2 - 14x - 14)$$

$$2x^2 - 4x + 15 - 20x^2 + 14x + 14$$

$$= -18x^2 + 10x + 29$$

⑥

$$(6a^8 \cdot b^7) \cdot (3a^4 \cdot b^3) = 6 \cdot 3 \cdot a^8 \cdot a^4 \cdot b^7 \cdot b^3$$

$$a^8 \cdot a^4 = a^{12}$$

$$b^7 \cdot b^3 = b^{10}$$

$$= 180a^{12} \cdot b^{10}$$

⑦

$$5x^4(x^2 + 3x - 4)$$

$$= 5x^6 + 15x^5 - 20x^4$$

$$\begin{matrix} 42 \\ x \cdot x \\ = x^6 \end{matrix}$$

⑧

$$(5x - 2) \cdot (x^2 + 3x + 2)$$

$$\begin{aligned} & 5x^3 + 15x^2 + 10x - 2x^2 - 6x - 4 \\ & = 5x^3 + 13x^2 + 4x - 4 \end{aligned}$$

(9.) $(x-7) \cdot (x-3)$
F O I L

$$x^2 - 3x - 7x + 21$$
$$= x^2 - 10x + 21$$

(10.) $(x+7)(x+7)$
F O I L

$$x^2 + 7x + 7x + 49$$
$$= x^2 + 14x + 49$$

(11.) $(x^2+2) \cdot (x-7)$
F O I L

$$x^3 - 7x^2 + 2x - 14$$

12.

$$(a) (x+4)^2$$

$$= (x+4)(x+4)$$

$$\begin{array}{cccc} F & O & I & L \\ x^2 & +4x & +4x & +16 \end{array}$$

$$= x^2 + 8x + 16$$

$$= x^2 + 8x + 16$$

$$(b) (1+3x) \cdot (1-5x^2)$$

$$\begin{array}{cccc} F & O & I & L \\ 1 & +3x & -5x^2 & \end{array}$$

$$1 - 5x^2 + 3x - 15x^3$$

$$= -15x^3 - 5x^2 + 3x + 1$$

$$(c) (x^2-3)^2 = (x^2-3)(x^2-3)$$

$$\begin{array}{cccc} F & O & I & L \\ x^4 & -3x^2 & -3x^2 & +9 \end{array} = x^4 - 6x^2 + 9$$

① $(n+7) \cdot (n-7)$

$$= n^2 - 7n + 7n - 49$$

Use: F O I L

$$= n^2 - 49$$

Note:

$$(n+7)(n-7) = n^2 - 7^2$$

$$(a+b)(a-b) = a^2 - b^2$$

② $(4n+7) \cdot (4n-7)$

F O I L

$$\begin{array}{r} 4^2 n^2 - 28n + 28n - 49 \\ (4n)^2 - 28n + 28n - 49 \end{array}$$

$$\hookrightarrow 16n^2 - 49$$

NOTE: $(4n+7)(4n-7)$

$$= (4n)^2 - 7^2$$

$$= 16n^2 - 49$$

$$(13) (2x^2y - 4xy + 15y) + (20x^2y + 14xy - 14y)$$

$$= 22x^2y + 10xy + y \text{ see } \textcircled{\#4}$$

$$(14) (2x^2y - 4xy + 15y) - (20x^2y - 14xy^2 - 14y)$$

$$= 2x^2y - 4xy + 15y - 20x^2y + 14xy^2 + 14y$$

$$= -18x^2y - 4xy + 29y + 14xy^2$$