

# Lab 3

## Statistics of Projective Motion

$$V_0 = \frac{x}{t}$$

$$H = \frac{1}{2} g t^2 \Rightarrow t = \sqrt{\frac{2H}{g}}$$

$$x_{th} = V_0 \cdot t = V_0 \sqrt{\frac{2H}{g}}$$

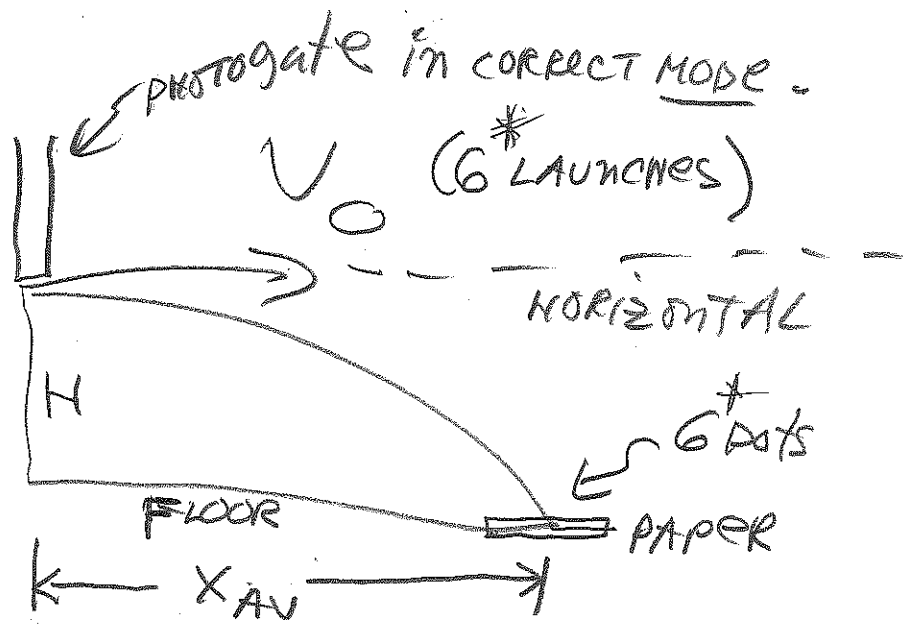
$$\Delta x_{th} \approx \frac{\partial x}{\partial V_0} \cdot \Delta V_0 + \frac{\partial x}{\partial H} \cdot \Delta H$$

$$\frac{\partial x}{\partial V_0} = \sqrt{\frac{2H}{g}} \quad \text{and} \quad \frac{\partial x}{\partial H} = V_0 \cdot \left[ \sqrt{\frac{2}{g}} \cdot \frac{1}{2} H^{-\frac{1}{2}} \right] = V_0 \cdot \sqrt{\frac{1}{2gH}}$$

$$\Delta x_{th} \approx \sqrt{\frac{2H}{g}} \cdot \Delta V_0 + V_0 \sqrt{\frac{1}{2gH}} \cdot \Delta H$$

MEASURE  $V_0$  6\* TIMES \*6 OR MORE

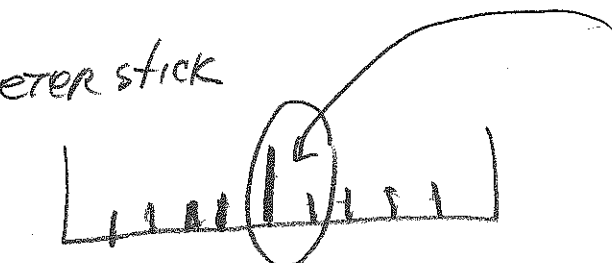
$$\Delta V_0 = \frac{V_{0MAX} - V_{0MIN}}{2} \quad \text{OR} \quad \text{STANDARD DEVIATION OF MEAN (STDM)}$$



MINIMUM ERROR:

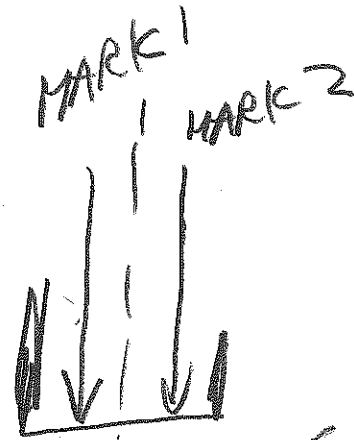
$$\Delta H = \frac{L.C.}{2}$$

METER STICK



100 cm

10 cm



100.5

100.6

L.C. = LEAST COUNT = 0.1 cm = 1 mm = 0.001 m

$$\text{MARK 1} = 100.56 \pm \frac{L.C.}{2}$$

$$(100.56 \pm 0.05) \text{ cm}$$

$$\text{MARK 2} = (100.60 \pm 0.05) \text{ cm}$$

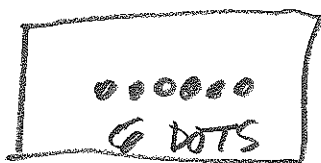
NOTE:  $X_{\text{EXP}} = X_{\text{AV}}$  (6\* DOTS)

CHECK

\* 6 OR MORE

$$|X_{\text{AV}} - X_{\text{TH}}| < \Delta X_{\text{TH}} + \Delta X_{\text{EXP}}$$

$$\Delta X_{\text{EXP}} = \frac{X_{\text{MAX}} - X_{\text{MIN}}}{2} \text{ OR standard deviation of mean}$$



PAPER ON FLOOR

NOTE:  $\Delta X_{TH}$  via QUADRATURE

$$\Delta X_{TH} = \sqrt{\left(\frac{\partial X}{\partial V_0} \cdot \Delta V_0\right)^2 + \left(\frac{\partial X}{\partial H} \cdot \Delta H\right)^2}$$

see penny state site.